Quantitative description of C$_{60}$ diffusion on an insulating surface

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The diffusion of C$_{60}$ molecules on large, atomically flat terraces of the CaF$_2$(111) surface is studied under ultrahigh vacuum conditions at various substrate temperatures below room temperature. The weak molecule-substrate interaction on this insulating surface makes a direct observation of hopping events difficult. Therefore, to determine a quantitative value of the diffusion barrier, we employ the so-called onset method. This method is based on the analysis of spatial properties of islands created by nucleation of diffusing C$_{60}$ molecules, as measured by noncontact atomic force microscopy. We first determine the critical cluster size to be $r^* \approx 1$ from coverage-dependent island size distributions prepared at a fixed substrate temperature. The diffusion barrier of $E_d = (214 \pm 16)$ meV and an attempt frequency of $\nu_0 = 1.4 \times 10^{12} \pm 0.6$ s$^{-1}$ are then obtained by analyzing the island densities at different substrate temperatures.

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I. INTRODUCTION

The concept of using organic molecules as building blocks for functional devices has attracted great interest since decades. A versatile strategy for building functional structures is molecular self-assembly. In particular, a detailed knowledge of both intermolecular as well as molecule-substrate interactions is required to control the growth process for successfully employing self-assembly techniques in device fabrication. The most important parameter for the migration of molecules on surfaces is the diffusion barrier and, consequently, several methods have been developed for the experimental determination of the diffusion barrier. The vast majority of these studies have, however, been performed using metallic rather than insulating substrates. This is largely due to the fact that most surface science-based analysis methods require conducting substrates. For application in molecular electronics, however, it is most desirable to arrange organic molecules on insulating rather than metallic surfaces in order to decouple the electronic structure of the molecular device from the substrate.

A widely used technique to study adsorbate diffusion is analyzing single hopping events. Using this technique, diffusion has extensively been studied for atomic species on metallic surfaces and results have been reviewed in Refs. 6, 8, and 10–13. Also for organic molecules on metal surfaces, the diffusion parameters were determined by direct observation of hopping events. These studies have revealed diffusion barriers for organic molecules on metallic substrates often being considerably larger than 800 meV, a barrier height that allows for monitoring single adsorbate jumps at room temperature. For instance, a value of 1400 meV has been found for diffusion of C$_{60}$ on Pd(110). In general, the diffusion barrier of organic molecules on insulating surfaces is much smaller than on metallic surfaces, as evidenced by a strong clustering of organic molecules on insulating surfaces. Due to the small diffusion barrier, monitoring of individual molecular jumps is, therefore, not feasible at room temperature. Moreover, in the case of small diffusion barriers, a direct observation of single hopping events may be influenced by the interaction between the imaging tip and the molecule, as observed in scanning tunneling microscopy and noncontact atomic force microscopy (NC-AFM) imaging.

In cases where a direct observation of single hopping events is not possible, the analysis of island densities at different growth temperatures (so-called onset method) has been proven to provide reliable values for the diffusion barrier. Using this technique, the diffusion barrier has been determined for a few molecular systems on metallic and semiconducting surfaces. On insulating surfaces, however, quantitative analysis of molecular diffusion has been performed very rarely so far, revealing diffusion barriers ranging from 100 to 400 meV. The latter experiments were, however, not accomplished under ultrahigh vacuum (UHV) conditions in all steps. Such experimental conditions result in an increased surface contamination and may, therefore, alter molecular diffusion and influence the island density and island size distribution.

In this work, we employ the onset method to determine the diffusion barrier and attempt frequency for the tracer diffusion of C$_{60}$ molecules on an insulating and atomically flat surface, namely, CaF$_2$(111). Our results reveal a diffusion barrier of $E_d = (214 \pm 16)$ meV for this system, much smaller than what is typically observed for C$_{60}$ molecules on metallic surfaces. In contrast to previously described studies of organic molecules on insulating surfaces, our work is performed under UHV conditions, revealing quantitative results that are not affected by surface contaminants.

II. EXPERIMENTAL METHODS

For our experiments, we use cleaved surfaces of high purity CaF$_2$ crystals (Korth Kristalle, Altenholz, Germany). Prior the experiments, crystals were outgased in UHV for 1.5 h at 425 K. After the sample had cooled down to room temperature, the crystal was cleaved in situ and heated again (1.5 h at 425 K) to remove charges trapped on the surface. The cleaved surface reveals atomically flat terraces with dimensions often larger than 4 $\mu$m$^2$ when applying a recently de-
III. ADSORPTION GEOMETRY

Figure 1(a) shows an overview image of C_{60} island formation on CaF_{2}(111) prepared at a substrate temperature of \( T_s = 169 \, \text{K} \). As can clearly be seen, all islands exhibit an overall hexagonal shape. The orientation of the islands with respect to the substrate reveals a grouping of islands into two different domains as illustrated in Fig. 1(a) by solid red and dashed blue hexagons, respectively. The sides of islands from different domains enclose an angle of \( 38^\circ \pm 2^\circ \), as shown in Fig. 1(b). In Fig. 1(c) a structural model for the possible arrangement of C_{60} molecules on the atomic lattice is presented that would result in an angle of 38.2° between the two domains. This model is in perfect agreement with previously presented results from Fölsch et al.\(^{40,41}\) who have studied the adsorption of C_{60} on the CaF_{2}(111) by means of reflection high-energy electron diffraction.

Assuming single jumps of molecules between the adsorption sites defined by this model, we define a single jump length of \( l = 386 \, \text{pm} \) (distance between two adsorption sites). The area of an adsorption site that is a hexagonal unit allowing a space-filling coverage of the surface without overlap amounts to \( \Omega = \sqrt{3}/2 l^2 = 1.29 \times 10^5 \, \text{pm}^2 \) (a single adsorbed C_{60} molecule covers about six adsorption sites). Jump length and adsorption site area are marked in Fig. 1(c).

When preparing islands at substrate temperatures larger than 220 K, C_{60} molecules appear to nucleate in the second layer, however, this will not be discussed here but in a forthcoming publication. The second layer occupation does arise from direct impinging molecules as well as from molecules dewetting from the surface to the second layer.\(^{20}\) To facilitate an unambiguous island size distribution analysis, care was taken to restrict the present study to single-layer islands. Thus, the present study is limited to substrate temperatures \( T_s \leq 220 \, \text{K} \) and coverages \( \theta \leq 0.28 \, \text{ML} \). In this regime, the islands exhibit only very few C_{60} molecules in the second layer as seen in tiny bright structures on top of islands in Figs. 1(a) and 1(b). At the highest temperature used here (217 K) the second layer occupation is 5% at 0.1 ML and rises to 14% for 0.28 ML. At all lower temperatures, the second layer occupation is smaller than 5% at a coverage of 0.1 ML.

IV. GROWTH MODEL

A. Island density

To determine the diffusion barrier \( E_d \) and the attempt frequency \( \nu_0 \) from island densities, a growth model has to be applied. For obtaining an analytical model describing nucleation and growth upon molecular deposition, some simplifying assumptions are made:\(^{18}\) (a) single molecules are the only mobile species and do not desorb from the surface (complete condensation). (b) In addition, a distinction between stable and unstable clusters is made, which implies a critical island size \( i^* \). Stable clusters with sizes \( a > i^* \) are not allowed to shrink but can further grow by capture of single molecules. Unstable clusters with size \( a \leq i^* \) are allowed to decay, i.e., \( i^* = 1 \) implies that dimers and all larger clusters are stable. Note, that the critical cluster size \( i^* \) depends on...
deposition parameters (such as flux $F$ and substrate temperature $T_s$ during deposition) and is not a constant intrinsic value for the molecules-substrate system.

With these assumptions, the following equation has been derived for the steady state nucleation regime: \cite{7,42-45}

$$
\dot{N} = 0.25 \left( \frac{\Omega^2 F}{D} \right) \frac{\ell^2}{i^2} \exp \left( - \frac{E_i}{i^2 + 2 k_B T_s} \right),
$$

where $\dot{N}$ is the number of islands per adsorption site, $\Omega$ is the area of one adsorption site, $F$ is the molecule flux, $k_B$ is the Boltzmann constant, $T_s$ is the substrate temperature and $E_i$ is the cluster binding energy gained in forming a cluster of size $i^*$. A cluster consisting of one molecule has no cluster binding energy, therefore $E_i = 0$. The diffusion coefficient $D$ in two dimensions is defined by \cite{10}

$$
D = \frac{1}{4} l^2 v_0 \exp \left( - \frac{E_d}{k_B T_s} \right),
$$

where $l$ is the distance between two adsorption sites covered in a single jump, $v_0$ is the attempt frequency and $E_d$ is the diffusion barrier.

Combining Eqs. (1) and (2) allows to reveal the diffusion barrier and the attempt frequency from the so-called onset experiment. A short outline of the onset experiment is given in the following. A small amount of atoms/molecules is deposited onto the surface, using a fixed flux $F$ and coverage $\theta$. During deposition, the substrate temperature $T_s$ is held at a fixed value (typically between room temperature and liquid-nitrogen or liquid-helium temperature). After deposition, the sample is quenched to a temperature, at which diffusion is entirely frozen and imaged by scanning probe microscopy. This experiment is carried out for different substrate temperatures $T_s$. For each experiment, the island density of the deposited species is counted and plotted against the substrate temperature $T_s$ at deposition. The slope $m$ of $\ln \dot{N}$ versus $T^{-1}$ determines the diffusion barrier to

$$
E_d = k_B T_s \frac{i^* + 2}{2} - \frac{E_i}{i^*},
$$

and the axis intercept $N_0 = \lim_{T_s \to 0} \dot{N}$ gives the attempt frequency

$$
v_0 = 4 F^2 \frac{\Omega^2}{L^2} \frac{0.25}{N_0} \exp \left( \frac{E_i}{i^*} \right).$$

For obtaining both values, the critical island size $i^*$ must be identified first. This can be done by analyzing the island size distributions, as described in the following section.

### B. Island size distribution

We consider the steady-state nucleation regime with an island size distribution $n_a$ ($n_a$ denotes the density of islands with size $a$). In this case the dynamic scaling hypothesis \cite{46-49} states that $n_a$ scales with the following three parameters: the coverage $\theta$, the mean island size $A$ and a scaling function $f_r(a/A)$

$$n_a = \theta A^2 f_r(a/A).$$

The scaling function depends solely on the critical island size and the ratio of $a/A$ but not on the coverage. Based on kinetic Monte Carlo simulations, an empirical function for $f_r(a/A)$ has been constructed \cite{50}

$$f_r(a/A) = c_r(a/A) \exp \left( - \frac{1}{a} b_r(a/A) \right),$$

where $c_r$ and $b_r$ are fixed through the normalization conditions

$$
\int_0^\infty f_r(a/A) da(a/A) = \int_0^\infty c_r(a/A) f_r(a/A) da(a/A) = 1.
$$

### C. Determining the critical island size

To obtain the critical island size from experiments, the island size distribution $n_a$ is analyzed for different coverages at a fixed temperature and compared to the theoretical island size distributions for different $i^*$ given by Eq. (6).

This was accomplished in a series of molecular adsorption experiments with coverages ranging from $\theta = 0.10$ ML to $\theta = 0.28$ ML performed at a substrate temperature of $T_s = 217$ K. Samples were quenched to 92 K for NC-AFM measurements. Island sizes were determined from topography images, using the threshold marking functionality from Gwyddion. Artifacts were manually removed before exporting the island size distributions. The island sizes may be shifted due to thermal drift, the size of the tip apex and feedback settings. These issues will be discussed in the following. To estimate the maximum error of drift effects, a rather large lateral drift of 0.1 nm/s for the slow scanning direction is assumed. Thus, for typical scanning parameters (frame size 3000 nm $\times$ 3000 nm and time 1000 s per frame) the relative error is about 3%. \cite{51} For the error arising from the size of the imaging tip, we assume a typical tip size of 10 nm. This yields a relative error of 0.4% at a frame size of 3000 nm $\times$ 3000 nm. Thus, the size of the tip is negligible for the analysis of large frames. Moreover, feedback settings may affect the apparent island size, e.g., with slow feedback settings the islands get elongated on the rear site along the fast scanning direction. In these cases, a comparison of the forward and backward scan clarified the outer shape of the island.

Figure 2 shows the data of the scaled island size distribution $n_a A^2 / \theta$ plotted against the normalized island size $a/A$ for three different coverages. As expected, the scaled data points lie on one smooth curve except for the deviations due to experimental errors. Scaling functions $f_r(a/A)$ were calculated for $i^* = 1, 2, 3$ according to Eq. (6). Clearly, the experimental data is best described by the model curve for $i^* = 1$ at $T_s = 217$ K. In other words, dimers and all larger clusters are stable at 217 K and are not assumed to decay.

### D. Determining the diffusion barrier and attempt frequency

Using the critical island size from the previous section, the diffusion barrier $E_d$ and the attempt frequency $v_0$ can now be determined exploiting the dependence of the island density on temperature. This has been accomplished by procedures described in the following.
strong evidence for a critical island size of \( i^* = 1 \). The island densities were obtained from a total of 1300

islands. We assume an error of \( \Delta N = 4\% \) for the island densities. In Fig. 4, \( \ln(N) \) versus \( T_S^{-1} \) is plotted and it can be seen that the data points follow a linear dependence. As the critical island size was determined to be \( i^* = 1 \) for 217 K and no distinct variations from the linear dependence are observed for lower temperatures from Fig. 4, we can safely assign \( i^* = 1 \) for island growth between 96 K and 217 K. From the slope of the linear regression of the data, a diffusion barrier of \( E_d = (214 \pm 16) \) meV is derived according to Eq. (3). The attempt frequency \( \nu_0 = 1.4 \times 10^{12 \pm 1.6} \) s\(^{-1}\) is taken from the axis intercept according to Eq. (4).

V. CONCLUSION

In summary, we analyzed the diffusion of \( C_{60} \) molecules on the atomically flat \( \text{CaF}_2(111) \) surface at various substrate temperatures under the clean conditions of an ultrahigh vacuum. At low temperatures, we observed the coexistence of two domains, with a hexagonal island shape.

For the determination of the diffusion parameters we analyzed island densities and island sizes instead of observing single-molecule hopping events. We determined the critical island size (\( i^* = 1 \)) and the diffusion barrier (\( E_d = (214 \pm 16) \) meV) for this system.

The value for the diffusion barrier agrees well with the general picture of a weak molecule-substrate interaction in the case of insulating surfaces (\( E_d \approx 400 \) meV).\(^{31-35}\) It is much lower than the diffusion barrier of \( C_{60} \) molecules on metal surfaces, e.g., 1400 meV on Pd(110).\(^{16}\) Moreover, the attempt frequency \( \nu_0 = 10^{12} \) s\(^{-1}\) lies within the range of previously reported values for large molecules (10\(^{10}\) to 10\(^{14}\) s\(^{-1}\)).\(^{14-16}\)

The knowledge of the diffusion barrier plays a major role in exploiting molecular arrangements at different temperatures. It is, for example, possible to tune the island density by varying the substrate temperature. Thereby, a specific density of uniformly shaped \( C_{60} \) clusters can be created, which is of great importance for future molecular electronics, e.g., for the use as nanopads.\(^{52}\)
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